UE PIC - Math Refresher Course<br>Resit exam<br>- Duration: 1h30 -

1) Compute the real and imaginary part of $z=\frac{(3+5 i)^{2}}{1-2 i}$.
2) Compute the trigonometric form of $z=1+i \sqrt{3}$ and then compute the real and imaginary part of $z^{6}$.
3) Compute the trigonometric form of $\frac{3+2 i}{2-i}$.
4) Check that $x=-1$ is a root of $x^{3}+2 x^{2}-11 x-12=0$. Compute all the roots.
5) Compute the partial fraction decomposition of:

$$
\frac{x^{4}}{x^{2}-1}
$$

6) Compute the following limits:

$$
\begin{gathered}
\lim _{x \rightarrow+\infty} \frac{x^{2}-x}{9 x^{5}-6 x^{2}+7} \\
\lim _{x \rightarrow 2} \frac{x^{2}-4}{x^{2}-3 x+2} \\
\lim _{x \rightarrow 3+} \frac{1-4 x}{x-3}
\end{gathered}
$$

7) Using the Laplace transform solve the following differential equation:

$$
\ddot{y}(t)+5 \dot{y}(t)+6 y(t)=0
$$

with: $\quad y\left(0^{-}\right)=2 \quad ; \quad \dot{y}\left(0^{-}\right)=3$

